

Figure 1

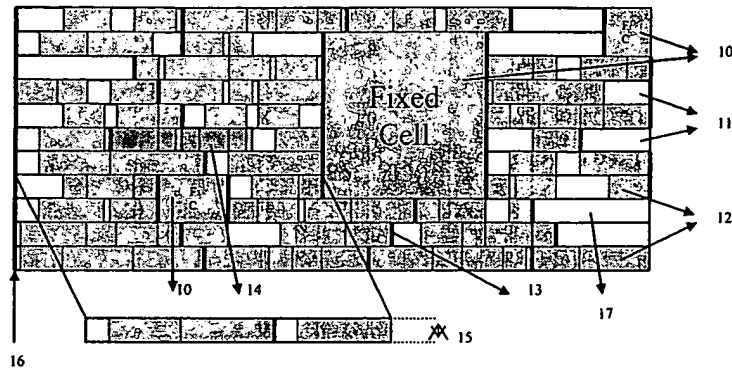


Figure 2

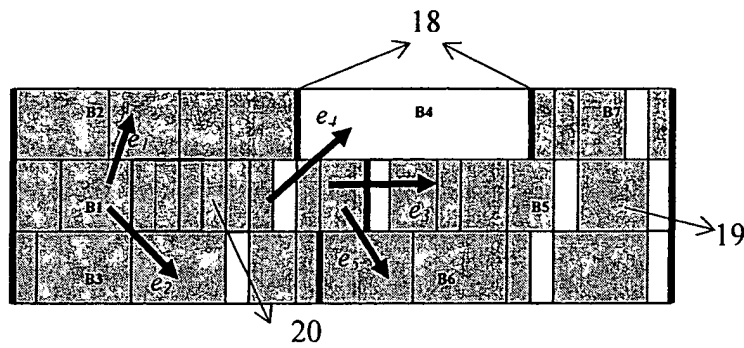
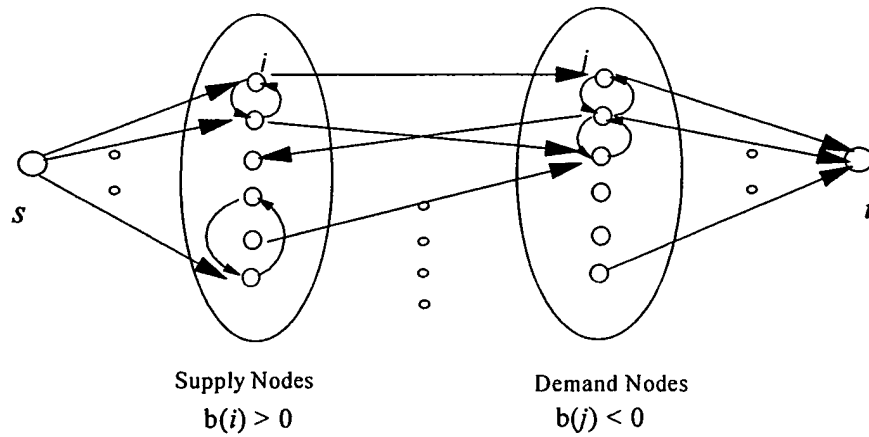


Figure 3



$\forall i$ if $b(i) > 0$,
 $\text{Cap}(e_{si}) = b(i)$
 $\text{Cost}(e_{si}) = 0$

$\forall i \neq s, j \neq t$,
 $\text{Cap}(e_{ij}) = \text{Infinity (Large Int)}$
 $\text{Cost}(e_{ij}) = K_{e_{ij}}$

$\forall j$ if $b(j) < 0$,
 $\text{Cap}(e_{jt}) = -b(j)$
 $\text{Cost}(e_{jt}) = 0$

\forall : Notation represents the meaning "For Every Element"
 \in : Notation represents the meaning "Element of"

Figure 4

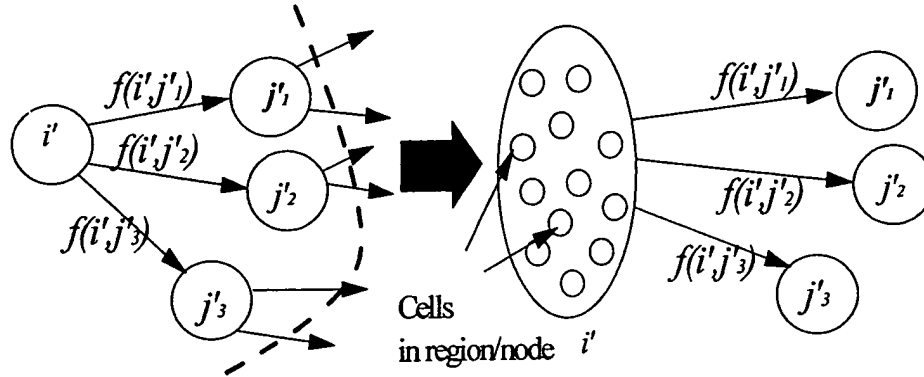
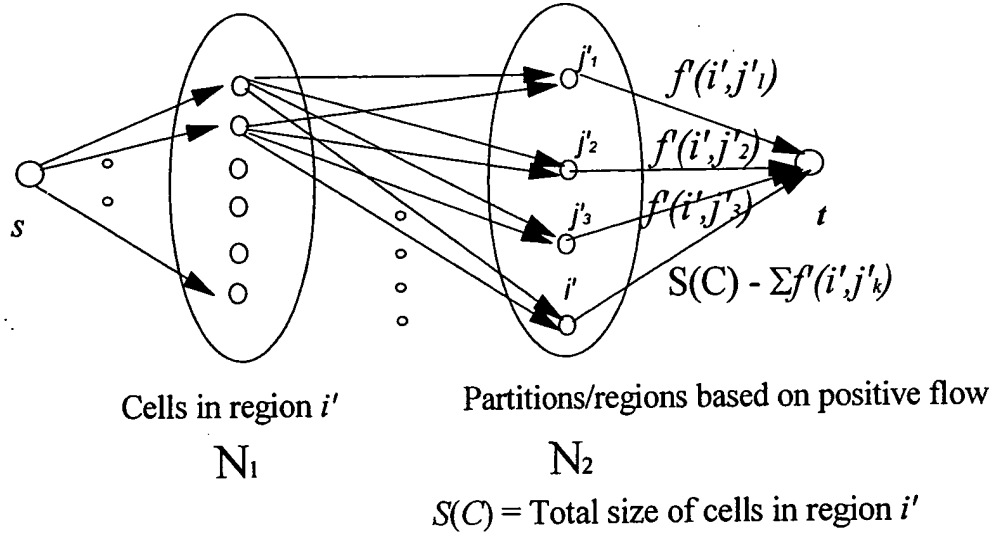


Figure 5



$$\begin{aligned} \forall i \in N_1 \\ \text{Cap}(e_{si}) &= 1 \\ \text{Cost}(e_{si}) &= 0 \end{aligned}$$

$$\begin{aligned} \forall i \in N_1, j \in N_2, \\ \text{Cap}(e_{ij}) &= 1 \\ \text{Cost}(e_{ij}) &= \text{Cost of moving} \\ &\quad \text{cell } i \text{ to region } j \\ \text{multiplier } \mu_{ij} &= \text{size of cell } i \end{aligned}$$

$$\begin{aligned} \forall j \in N_2 \\ \text{Cap}(e_{jt}) &= \text{flow to region } j \\ \text{Cost}(e_{jt}) &= 0 \end{aligned}$$

\forall : Notation represents the meaning "For Every Element"
 \in : Notation represents the meaning "Element of"

Figure 6

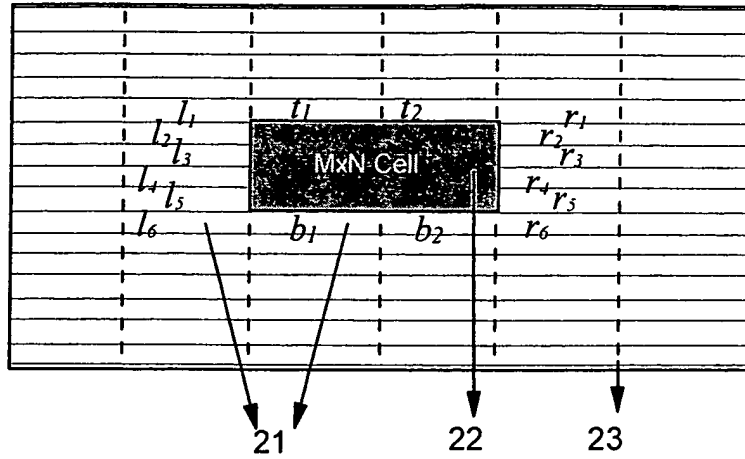
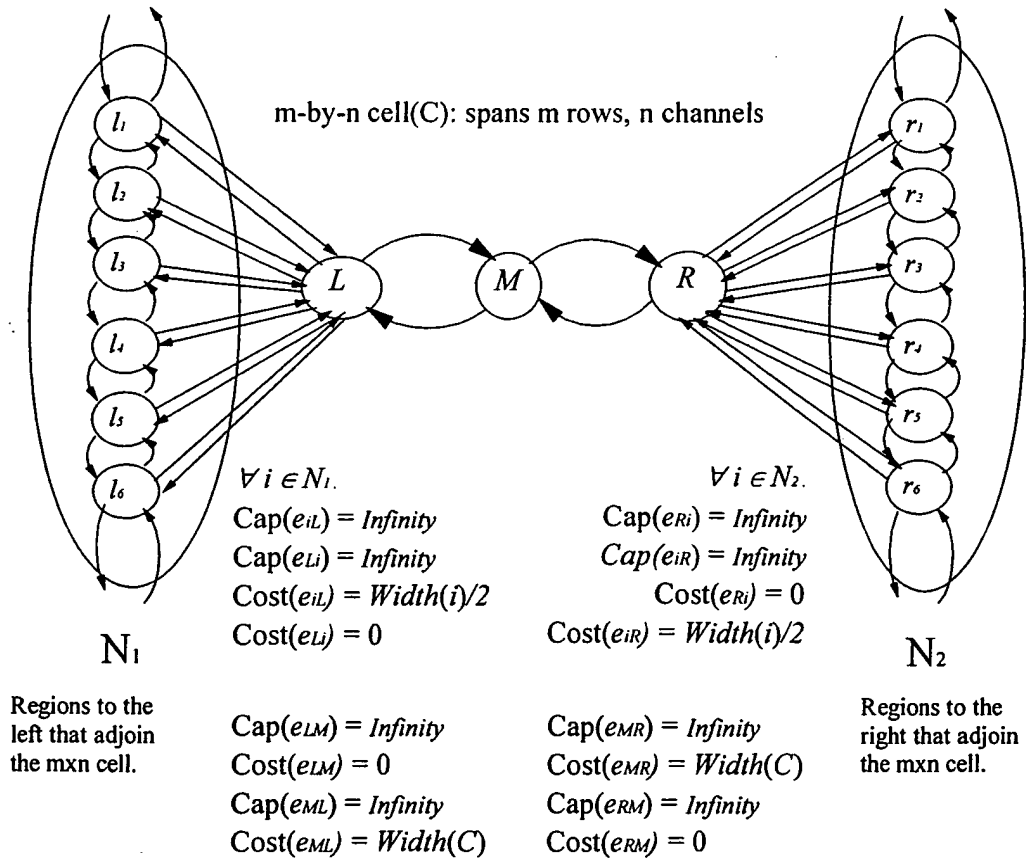


Figure 7



\forall : Notation represents the meaning "For Every Element"

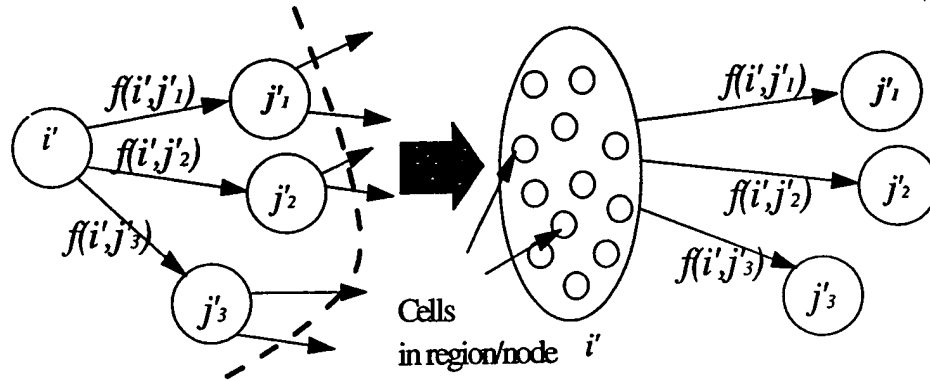
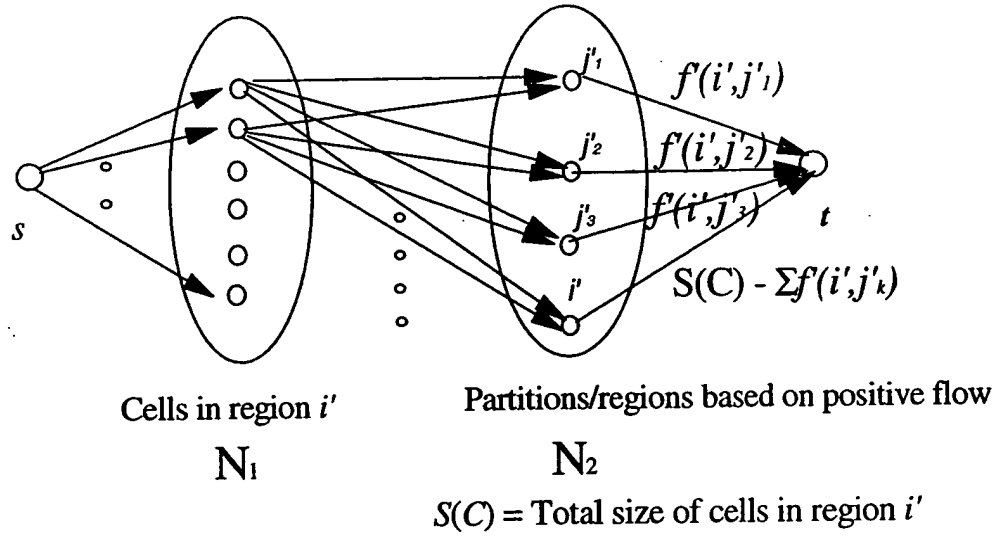


Figure 5



$\forall i \in N_1$
 $\text{Cap}(e_{si}) = 1$
 $\text{Cost}(e_{si}) = 0$

$\forall i \in N_1, j \in N_2,$
 $\text{Cap}(e_{ij}) = 1$
 $\text{Cost}(e_{ij}) = \text{Cost of moving}$
 $\text{cell } i \text{ to region } j$
 $\text{multiplier } \mu_{ij} = \text{size of cell } i$

$\forall j \in N_2$
 $\text{Cap}(e_{jt}) = \text{flow to region } j$
 $\text{Cost}(e_{jt}) = 0$

\forall : Notation represents the meaning "For Every Element"
 \in : Notation represents the meaning "Element of"

Figure 6

```

Placement_Aware_Region_Definition ()
Begin
  1 Build placement image
  2 For each circuit row  $r$  in the layout
    Begin
      3  $scanline\_x = row\_xlow(r); last\_region\_boundary = row\_xlow(r);$ 
      4  $leading\_free\_space = false;$ 
      5  $S =$  sorted list of cells in row  $r$  by increasing position along  $x$ -direction
      6  $c =$  first cell in sorted list  $S$ 
      while ( $c$ )
        Begin
          7 If ( $xpos(c) > scanline\_x$ )
            Begin
              8 If ( $xpos(c) - last\_region\_boundary > W$ )
                Begin
                  9  $p = create\_region(r, last\_region\_boundary + W, last\_region\_boundary)$ 
                  10  $scanline\_x = (last\_region\_boundary + W)$ 
                End
              11 Else
                Begin
                  12 If ( $is\_fixed\_cell(c) \parallel is\_blockage(c) \parallel leading\_free\_space$ )
                    Begin
                      13  $p = create\_region(r, xpos(c), last\_region\_boundary)$ 
                      14  $scanline\_x = last\_region\_boundary = xpos(c)$ 
                      15  $leading\_free\_space = false$ 
                    End
                  16 Else if ( $xpos(c) - scanline\_x \geq 0.50 * W$  and  $scanline\_x > last\_region\_boundary$ )
                    Begin
                      17  $p = create\_region(r, scanline\_x, last\_region\_boundary)$ 
                      18  $last\_region\_boundary = scanline\_x$ 
                      19  $leading\_free\_space = true$ 
                    End
                  20 Else  $scanline\_x = xpos(c)$ 
                End
              21 End
            Else if ( $xpos(c) == scanline\_x$ )
              Begin
                22 If ( $is\_fixed\_cell(c) \parallel is\_blockage(c)$ )
                  Begin
                    23  $p = create\_region(r, xpos(c) + width(c), scanline\_x)$ 
                    24  $scanline\_x += width(c)$ 
                    25  $last\_region\_boundary = scanline\_x$ 
                  End
                26 Else if ( $is\_movable\_cell(c)$ )
                  Begin
                    27 If ( $xpos(c) + width(c) \leq W$ )
                      28  $scanline\_x += width(c)$ 
                    29 Else
                      Begin
                        30  $p = create\_region(r, xpos(c) + width(c), last\_region\_boundary)$ 
                        31  $last\_region\_boundary = scanline\_x$ 
                        32  $scanline\_x += width(c)$ 
                      End
                    End
                33  $c =$  next cell in the sorted list  $S$ 
              End
            End
          End
        End
      End
    End
  End

```

FIGURE 9

Global_Area_Migration_Graph ($G(V,E)$)**Begin**

1. $V = \{\text{regions}\}$, $E = \{\text{edge between neighboring regions}\}$
2. $\forall e \in E$, $\text{Cost}(e) = K_e$
3. $\forall e \in E$, $\text{Cap}(e) = \text{Infinity}$ (Large integer)
4. $\forall v \in V$, $\text{Size}(v) = \text{Total size of movable cells in } v$
5. $\forall v \in V$, $\text{Cap}(v) = \text{Total available space for movable cells in } v \text{ (i.e. region)}$
6. $\forall v \in V$, $b(v) = \text{Size}(v) - \text{Cap}(v)$
7. If $b(v) > 0$, v is a supply node.
8. If $b(v) < 0$, v is a demand node.
9. If $b(v) = 0$, v is a transshipment node.

End

\forall : Notation represents the meaning "*For Every Element*"

\in : Notation represents the meaning "*Element of*"

Figure 10

Generalized_Flow_Graph (region i')**Begin**

1. $N_1 = \{\text{cells in region } i'\}, N_2 = \{i'\} \cup \{\text{neighboring regions}\}$
2. $E = \{\text{edge representing cell-to-region assignment}\}$
3. $S(N_1) = \text{Total size of cells in } N_1 \text{ (region } i')$
4. $\text{Smallest}(N_1) = \text{Smallest cell size in } N_1 \text{ (region } i')$
5. *Introduce an edge from N_1 to N_2 for every possible cell-to-region assignment,*
 $\forall i \in N_1, j \in N_2, \text{Cap}(e_{ij}) = 1$
 $\forall i \in N_1, j \in N_2, \text{multiplier}, \mu_{ij} = \text{size of cell } i$
 $\forall i \in N_1, j \in N_2, \text{Cost}(e_{ij}) = \text{Cost of moving cell } i \text{ to region } j$
6. *Introduce source node s , with edges such that*
 $\forall i \in N_1, \text{Cap}(e_{si}) = 1$
 $\forall i \in N_1, \text{Cost}(e_{si}) = 0$
7. *Introduce sink node t , with edges such that*
 $\forall j \in N_2, \text{Cap}(e_{jt}) = f(i', j) = \text{MAX}(\text{Smallest}(N_1), f(i', j)), \text{ If } f(i', j) > 0$
 $0, \text{ Otherwise}$
 $\forall j \in N_2, \text{Cost}(e_{jt}) = 0$

End

\forall : Notation represents the meaning "For every element"

\in : Notation represents the meaning "Element of" (a set theory notation)

Figure 11